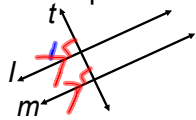
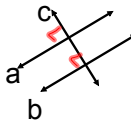
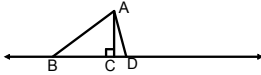


Warmup!

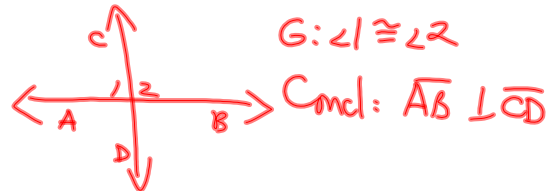
Given:  $l \parallel m$ ;  $l \perp t$ 1. Conclusion:  $m \perp t$ Given:  $a \perp c$ ;  $b \perp c$ 2. Conclusion:  $a \parallel b$ 3. Which segment(s) represent distance from A to  $\overline{CB}$ ? $\overline{AC}$ 

## 3.6 Prove Theorems about Perpendicular Lines

Notes

Several theorems about perpendicular lines

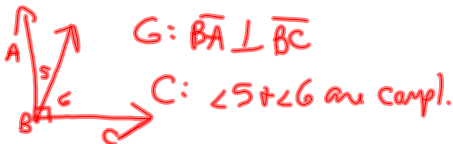
Theorem 3.8—If 2 lines intersect to form a linear pair of congruent angles, then the lines are perpendicular.



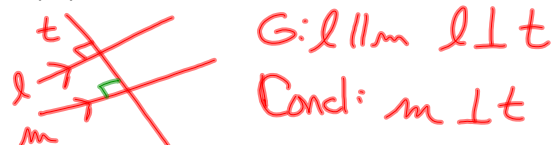
Theorem 3.9—If 2 lines are perpendicular, then they intersect to form four right angles.

(def of  $\perp$ )  $l \perp m$   $\xrightarrow{\text{m. 4/2}} G: l \perp m$   
 Concl:  $\angle 1, \angle 2, \angle 3, \angle 4$  are right  $\angle$ s

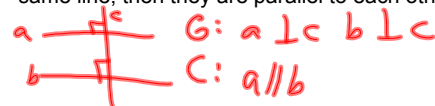
The Complement Theorem—If 2 sides of 2 adjacent acute angles are perpendicular, then the angles are complementary.



Theorem 3.11—Perpendicular Transversal Theorem—If a transversal is perpendicular to one of two parallel lines, then it is perpendicular to the other.



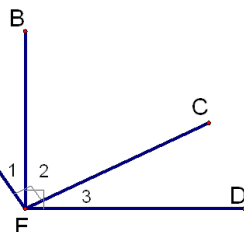
Theorem 3.12—Lines Perpendicular to a Transversal Theorem—In a plane, if two lines are perpendicular to the same line, then they are parallel to each other.



Example:

Given:  $\overline{AE} \perp \overline{EC}$ ;  $\overline{BE} \perp \overline{ED}$ Prove:  $\angle 1 \cong \angle 3$ 

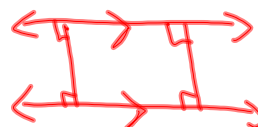
Statements	Reasons
① $\overline{AE} \perp \overline{EC}$ $\overline{BE} \perp \overline{ED}$	① Given
② $\angle 1 + \angle 2$ are compl $\angle 2 + \angle 3$ are compl	② The Compl. thm
③ $\angle 1 \cong \angle 3$	③ $\cong$ Compl. thm



Distance from a point to a line—the length of the perpendicular segment from the point to the line.



The distance between 2 parallel lines is the length of any perpendicular segment joining the 2 lines.



Examples:

Find the distance between the point and the line listed.

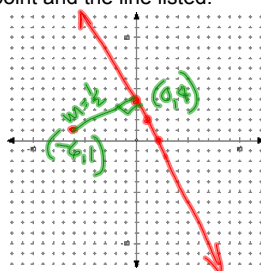
Ex 1:  $(-6, 1)$  and  $y = -2x + 4$ 

$$y = +\frac{1}{2}x + b$$

$$1 = \frac{1}{2}(-6) + b$$

$$4 = b$$

$$y = \frac{1}{2}x + 4$$



$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\sqrt{45}$$

$$= 3\sqrt{5} \approx 6.71 \text{ units}$$

Ex 2:  $(3, 0)$  and

$$y = \frac{2}{3}x + 4$$

① Find eqn of line containing  $\perp$  segment

$$y = -\frac{3}{2}x + b$$

$$0 = -\frac{3}{2}(3) + b$$

$$\frac{9}{2} = b$$

$$y = -\frac{3}{2}x + \frac{9}{2}$$

② Solve the system

$$\begin{cases} \frac{2}{3}x + 4 = -\frac{3}{2}x + \frac{9}{2} \\ 4x + 24 = -9x + 27 \end{cases}$$

$$4x + 24 = -9x + 27$$

③ Distance

Formula  
(w/ new pt + original pt)

$$d = \sqrt{\left(3 - \frac{3}{13}\right)^2 + \left(0 - \frac{54}{13}\right)^2} = \sqrt{\frac{16}{169} + \frac{2916}{169}} = \sqrt{\frac{2932}{169}} = \frac{\sqrt{2932}}{13} \approx 4.99$$

$$y = \frac{2}{3}x + 4$$

$$\frac{2}{3}x + 4 = 3$$

$$\frac{2}{3}x = -1$$

$$x = -\frac{3}{2}$$

Find the distance between the two parallel lines.

Ex 3:  $y = 3x + 5$  and  $y = 3x - 2$ 

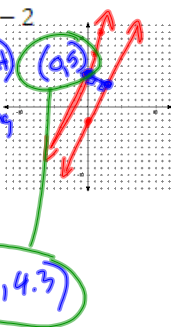
① Pick a pt (one of the 2 y-int)

② Find the eqn. of line containing  $\perp$  segment

$$y = -\frac{1}{3}x + 5$$

③ Find the intersection

$$\begin{cases} y = -\frac{1}{3}x + 5 \\ y = 3x - 2 \end{cases}$$

④ Distance  
 $d \approx 2.21$ Ex 4:  $y = \frac{-1}{2}x$  and  $y = \frac{-1}{2}x + 6$ 

Find the equation of the perpendicular bisector of the segment with the given endpoints.

Ex 5:  $(5, 2)$   $(3, -6)$ Ex 6:  $(-3, 7)$   $(8, -5)$

HW p194-195 #s 1-7, 13-17  
and find the distance between

last 3  
from sheet

$$y = -2x + 4$$

$$y = -2x - 5$$

Test Monday !

3.6 day 2 assignment

1. Find the distance between:

$$y = -2x - 5 \quad y = -2x + 4$$

2. Find the distance between:

$$y = 1.5x + 4 \quad y = 1.5x - 0.5$$

3. Parallelogram ABCD A(-4, -1) B(2, 3)

C(7, 2) D(1, -2) Find the distance between  
the parallel sides.

4. Find the equation of the perpendicular  
bisector of  $\overline{AB}$  A(0, 2) B(4, 7)